

1. **Multiple choice (20 points, 4 points each)** Please tick (*Kryssa för*) the correct answer. Only one answer is correct.
- (a) (4 points) In the naïve regression $Y_i = \beta_0 + \beta_1 X_i + u_i$, where the causal relationship of interest is the effect of X_i on Y_i , what can β_1 capture?
- The causal effect of X_i on Y_i
 - Reverse causality (the effect of Y_i on X_i)
 - Omitted variables bias (the correlation between Y_i and X_i that results from an omitted variable W_i affecting both X_i and Y_i)
 - All of the above
- (b) (4 points) Say we estimate the naïve regression $Y_i = \beta_0 + \beta_1 X_i + u_i$, where the causal relationship of interest is the effect of X_i on Y_i . If there is an omitted variable W_i which is positively correlated with X_i and has a negative effect on Y_i , what is the sign of the omitted variables bias in β_1 ?
- Positive
 - Negative
 - It does not create bias in β_1
 - There is not enough information to determine the sign of the bias.
- (c) (4 points) Say I randomly assign a treatment variable X_i to individuals, and measure the outcome Y_i . If I run the regression $\ln Y_i = \beta_0 + \beta_1 \ln X_i + u_i$, how do I interpret the coefficient β_1 ?
- A 1 unit change in X_i yields a change in Y_i of β units.
 - A 1 unit change in X_i yields a change in Y_i of $\beta \times 100\%$.
 - A 1% change in X_i yields a change in Y_i of $\beta \times 0.01$ units.
 - A 1% change in X_i yields a change in Y_i of $\beta\%$ units.
- (d) (4 points) Say I randomly assign a treatment variable X_i to individuals, and measure the outcome Y_i . If I run the regression $Y_i = \beta_0 + \beta_1 X_i + \beta_2 X_i^2 + u_i$, what is the expected change in Y_i from changing from $X_i = 2$ to $X_i = 3$?
- β_1
 - β_2
 - $\beta_1 + 5 \times \beta_2$
 - $2 \times \beta_1 + \beta_2$
- (e) (4 points) Say I randomly assign a treatment program to individuals. If they receive treatment, $T_i = 1$. Otherwise, $T_i = 0$. I measure the outcome Y_i . Y_i is a binary outcome variable i.e. it can only take the values 0 and 1. If I run the regression $Y_i = \beta_0 + \beta_1 T_i + u_i$, how do I interpret the coefficient β_0 ?
- $P(Y_i = 0)$ in the control group (for whom $T_i = 0$)
 - $P(Y_i = 0)$ in the treated group (for whom $T_i = 1$)
 - $P(Y_i = 1)$ in the control group (for whom $T_i = 0$)
 - $P(Y_i = 1)$ in the treated group (for whom $T_i = 1$)

2. **Multiple choice (20 points, 4 points each)** Please tick (*Kryssa för*) the correct answer. Only one answer is correct.
- (a) (4 points) I ran an experiment in 90 *Gymnasieskolor* in Stockholm, providing voluntary after school tuition programs in 45 of those schools, which I randomly selected. I collected data on exam results for all the students in those schools. In total, there were 36,000 students in my study. I want to evaluate the effect of the program. How should I treat my standard errors?
- a) I can assume standard errors are homoskedastic, and use the STATA default standard errors.
 - b) I should assume standard errors are heteroskedastic, and use STATA's robust option.
 - c) I should assume students who study at the same school are more similar to each other than students from different schools, and since all the students at a school have the same treatment status, I should *not* assume independence among observations and I should cluster standard errors by school.
 - d) I should assume that students who receive the tuition program will differ from those who don't receive the tuition program, so I should *not* assume independence among the treated and control group and I should cluster standard errors by whether or not the school received the treatment program.
- (b) (4 points) In analyzing my after-school tuition program experiment, I include a control for hours studied each week. Before I include this control, I see a strong positive effect of the tuition program on test scores. When I include this control, the result disappears. How should I interpret these regressions?
- a) The tuition program didn't really have any effect on test scores.
 - b) Hours studied each week is a bad control, because the tuition program could have affected the number of hours studied. These results shouldn't change our beliefs about whether the program increased test scores or not.
 - c) Leaving out hours studied each week creates omitted variable bias.
 - d) There was a problem with my randomization design.
- (c) (4 points) I want to estimate the effects of a randomly assigned program to increase access to safe drinking water. At baseline, 21% of households in the control group have access to safe drinking water, and 23% of households in the treated group have access to safe drinking water. At follow-up, 22% of households in the control group have access to safe drinking water, while 45% of households in the treated group have access to safe drinking water. Calculate the difference-in-difference estimate of the effect of the program on access to safe drinking water.
- a) 21%
 - b) 22%
 - c) 23%
 - d) 45%
- (d) (4 points) Oh no, termites ate my data! Some of my paper questionnaires got eaten by termites before I was able to enter the data into the computer. Before the termites got in, I had a representative sample of the population. Assuming the termites ate questionnaires at random, what is the consequence?
- a) The results of the study will be biased towards zero by measurement error.
 - b) The results of the study will be biased by measurement error, but the direction of the bias is unclear.
 - c) The results of the study will be unbiased, but less precisely estimated, because of having a smaller sample size.
 - d) The results of the study will be unbiased and more precisely estimated.

- (e) (4 points) I am interested in the causal effect of X_i on Y_i . I have a valid and relevant instrument Z_i . I use Z_i to predict X_i by estimating the first stage equation: $X_i = \gamma_0 + \gamma_1 Z_i + \nu_i$. The estimate of γ_1 is 4. Then I estimate the reduced form equation $Y_i = \pi_0 + \pi_1 Z_i + \epsilon_i$. The estimate of π_1 is 8. What is the IV estimate of the effect of X_i on Y_i ?
- a) 0.5
 - b) 2
 - c) 12
 - d) There is not enough information to calculate the answer.

3. **Interpreting the results of a regression (20 points)** Say I carried out an experiment among the 600 students of Econ 101. I assigned half of them to specific study groups, and asked them to meet each week to study together. I assigned the rest of the students to the control group.

I gave all the students a preliminary exam in the first week of the semester ($t = 0$), before I assigned treated students to study groups, and then collected all the students grades on the finals ($t = 1$). For each student, I therefore measure their pre-treatment grade, $GRADE_{i0}$ and their follow-up grade $GRADE_{i1}$. So I have two observations per student. Then I run the following regression:

$$GRADE_{it} = \beta_0 + \beta_1 FINAL_{it} + \beta_2 TREATED_{it} + \beta_3 FINAL_{it} \times TREATED_{it} + u_{it}$$

where $FINAL_{it}$ is equal to 0 for the preliminary exam, and 1 for the final exam, and $TREATED_{it}$ is equal to 0 for students in the control group, and 1 for students in the treated group.

- (a) How do I interpret the following coefficients?
- i. (2 points) β_0 ?
 - ii. (2 points) β_1 ?
 - iii. (2 points) β_2 ?
 - iv. (2 points) β_3 ?
- (b) I estimate this regression, and recover the following coefficients:

Coefficient	Estimate
β_0	0.47
β_1	0.16
β_2	-0.02
β_3	0.14

Calculate the following:

- i. (2 points) The mean score on the preliminary exam in the control group.
 - ii. (2 points) The mean score on the preliminary exam in the treated group.
 - iii. (2 points) The mean score on the final exam in the control group.
 - iv. (2 points) The mean score on the final exam in the treated group.
- (c) Say that I calculate, instead, the change in scores between the preliminary exam and final exam, for each student i.e. $\Delta GRADE_i = GRADE_{i1} - GRADE_{i0}$. Then I run the following regression:

$$\Delta GRADE_i = \alpha_0 + \alpha_1 TREATED_i + \epsilon_{it}$$

What will be my estimate of:

- i. (2 points) α_0
- ii. (2 points) α_1

4. **Panel data (20 points)** Say I would like to understand more about the effect of temperature on economic production. In particular, I would like to know about the effect of temperature on agricultural production. I have data on agricultural production (measured in dollars) for most countries in the world, for more than 40 years. I also have yearly mean temperature in each country.

(a) (4 points) I write down the following regression:

$$AGPROD_{it} = \beta_0 + \beta_1 TEMP_{it} + u_{it}$$

where $AGPROD_{it}$ is agricultural production in country i in year t , and $TEMP_{it}$ is the mean temperature in country i in year t . Does the coefficient β_1 have a causal interpretation? Why, or why not?

- (b) (4 points) Write down an alternative regression that you think would give a causal estimate.
- (c) (4 points) What must be true (what assumption needs to hold) in order for us to interpret the coefficient from your regression as a causal relationship? You may give your answer in words or using mathematical notation.
- (d) (4 points) Do you think it's reasonable to believe that this assumption holds in this case? Why or why not?
- (e) (4 points) Referring to a paper we discussed in class, why might it be important to consider non-linearity in this analysis? (You do not need to give the names of the authors or title of the paper if you do not remember them).

5. **Analysis using policies with thresholds (20 points)** Say I enroll the 600 students in Econ 101 in a second study. I use the results of the preliminary exam I asked them to take in the first week. All students who score below 50% on the exam will receive 2 hours of extra tuition every week. Students who score higher than 50% on the exam will not receive any extra tuition. I also have data on student characteristics at the start of class, including but not limited to grades in high school, parental income, gender, and date of birth.

- (a) (3 points) How might I measure the causal effect of the tuition program on student grades in the final?
- (b) (3 points) Explain using words why the method you propose should recover a causal estimate.
- (c) (6 points) What graphical (visual) evidence could I provide to demonstrate the effect of the program? You may provide a sketch or give a description in words of what you would do.
- (d) (4 points) What evidence could I provide to support the case that the effect I measured was a causal relationship?
- (e) (4 points) What specific concerns would you have about whether this was a causal relationship or not, and how could you provide evidence to evaluate the concern? *Hint: Assume I announced the program before I administered the test, and think about bunching.*